

REGIONAL VARIATIONS IN THE STRUCTURE OF THE CRUST IN THE CENTRAL UNITED STATES FROM *P*-WAVE SPECTRA

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ABSTRACT

Regional variations in the crustal structure in the central United States have been inferred by the transfer ratio method from an analysis of long-period *P* waves recorded at SHA, OXF, FLO and MDS, the stations nearly along 89°W longitude. The crustal structure in this region is approximated by a stack of horizontal parallel layers except possibly in the area around FLO, where the structure is rather complicated. The crustal thickness is predominantly controlled by the thick silicic upper crust, whereas the mafic lower crust is about 10 km thick throughout this region. The *P*-wave velocity of the lower crust is about 6.9 to 7.0 km/sec except probably in the area around FLO, where 7.4 km/sec velocity is more likely. A sedimentary layer with a velocity of about 3.0 km/sec, having a thickness of about 3 km near the coast of the Gulf of Mexico, tapers out to the north within the Gulf Coastal Plain. Deep discontinuities in the crust may be replaced by transitional layers up to 10 km thick. The Moho is about 33 km deep near the coast of the Gulf of Mexico, deepens to about 41 km near an intersection of the Gulf coastal plain and the interior plain, reaches about 47 km or more in the midst of the interior plain, and rises to about 41 km toward an intersection of the interior plain and the superior upland. As for the midst of the interior plain, however, the depth of the Moho reduces by as much as 5 km, if the velocity in the lower crust is about 7.0 km/sec instead of about 7.4 km/sec. In any case, the general trend of the depth of the Moho may match with the topographic feature from the Gulf of Mexico to Lake Superior.

INTRODUCTION

The crustal structure in the central United States is studied from an analysis of long-period *P* waves. This region is selected for the detailed study, because of the likelihood that the layering is simple there. This study corresponds to the first step of a two-step procedure formulated in Kurita (1973a). The formulation was a development of the transfer ratio method of Phinney (1964), which was based on the Thomson-Haskell matrix method.

DATA

Data are selected from all available film chips of the WWSSN long-period seismograms of SHA, OXF, FLO, and MDS. In order to study regional variations in crustal structure around these stations, we utilize records of shallow earthquakes which occurred at various azimuths from the station as well as those of deep earthquakes. As apparent from Figure 1, most of the earthquakes are differentiated into three groups according to the direction of wave approach: northwestern America, northeastern Asia (Alaska, Aleutian, Kurile, Japan); southwestern Asia, southeastern Europe (Turkey, Aegean Sea, Greece); and South America. Therefore, these earthquakes are tabulated separately in Tables 1, 2, and 3. Since the above three groups are almost concerned with the structure under the sector nearly northwest, northeast, and southeast of the station, they will be referred to as the NW, NE, and SE groups or sectors, respectively.

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TABLE 1
LIST OF EARTHQUAKES IN NORTHWESTERN AMERICA, NORTHEASTERN ASIA GROUP*

Shock Code	Origin			Time			Coordinates		D (km)	M	Location	Station	Delta (deg)	Azimuth (deg)	Angle of Incidence† (deg)	Later Phase‡ (sec)	T ₁ § (sec)	T ₂ (sec)	Component¶
	y	m	d	h	m	s	Lat. (deg)	Long. (deg)											
NW 1	70	04	16	05	33	17.5	59.8N	142.6W	7	5.5	Gulf of Alaska	FLO	38.7	320.3	37.6		80	40	ZNEM
NW 2	67	07	01	23	10	07.2	54.4N	158.0W	33	6.2	South of Alaska	SHA	54.2	317.4	32.0	PcP 64	80	40	ZNEM
											OXF	50.7	315.3	33.2	PcP 77	80	40	ZNE	
											FLO	47.1	312.5	34.4	PcP 92	80	40	ZNE	
NW 3	65	02	06	01	40	33.2	53.2N	161.9W	33	6.4	South of Alaska	MDS	47.1	308.5	34.4		80	40	ZNEM
NW 4	66	08	07	02	13	04.7	50.6N	171.2W	33	6.2	Aleutian Islands	FLO	55.9	310.6	31.4	PcP 58	80	34	ZNE
											MDS	53.4	308.3	32.1	PcP 71	80	36	ZNE	
NW 5	70	02	28	10	52	31.2	52.7N	175.1W	162	6.1	Andreanof Islands	OXF	61.0	316.0	29.3	pP 37	80	32	ZNEM
NW 6	69	05	14	19	32	54.2	51.3N	179.9W	21	6.2	Andreanof Islands	SHA	67.7	317.3	27.5	PcP 28	80	40	ZNEM
NW 7	65	10	01	08	52	04.4	50.1N	178.2E	23	6.3	Rat Islands	MDS	59.6	311.7	30.1	PcP 51	80	40	ZNE
NW 8	70	03	19	23	33	29.1	51.3N	173.8E	16	5.8	Near Islands	SHA	71.4	319.0	26.1	PcP 20	80	40	ZNEM
NW 9	70	05	27	12	05	06.0	27.2N	140.1E	382	6.2	Bonin Islands	FLO	64.2	316.1	28.6	PcP 36	80	34	ZNEM
											SHA	106.3	316.2	19.3		80	40	ZNEM	
											OXF	102.8	316.0	19.3		80	40	XNEM	
NW 10	68	10	07	19	20	20.3	26.3N	140.6E	516	6.1	Bonin Islands	FLO	99.2	315.9	19.3		80	40	ZNEM
											SHA	106.6	315.2	19.3		80	40	ZN M	
											OXF	103.2	315.1	19.3		80	40	ZNEM	
NW 11	64	05	02	16	11	00.2	45.5N	150.3E	35	5.7	Kurile Islands	MDS	76.7	321.2	24.2		80	40	ZNE
NW 12	68	04	01	00	42	04.2	32.5N	132.2E	33		Shikoku	FLO	98.8	324.7	19.3		80	40	ZNE
NW 13	69	01	19	07	02	04.4	45.0N	143.2E	204	6.4	Hokkaido	SHA	91.4	326.3	19.7	pP 49	80	40	ZNEM
											OXF	87.6	325.7	20.3	sP 72	80	40	ZNEM	
NW 14	69	12	18	13	32	05.2	46.3N	142.5E	344G	5.9	Sakhalin Island	OXF	87.0	326.9	20.3	pP 81	80	40	ZN M
NW 15	63	02	13	08	50	04.5	24.5N	122.1E	47		Taiwan Region	MDS	106.4	329.9	19.3		80	40	ZEM
NW 16	64	08	25	13	47	20.6	78.2N	126.6E	50	6.1	East of Severnaya Zemlya	OXF	65.5	352.4	28.0	PcP 34	80	36	ZN

* Information on these earthquakes is from the Earthquake Data Reports of the USCGS.

† Angle of incidence at the Moho, assumed to be 40 km deep, is calculated from the angle of incidence at the focus obtained by Banghar (1970), based on tables for *P* phases of Herrin *et al.* (1968).

‡ Later phases and their time differences from the direct *P* phase: *PcP-P*, *pP-P*, and *PP-P*, Herrin *et al.* (1968); *sP-P*, Jeffreys and Shimschoni (1964). Phases are generally not shown when their time differences are shorter than about 20 sec or longer than the relevant window length.

§ Time length of data window, $w_1(t)$.

|| Time length of data window, $w_2(t)$.

¶ Component of seismogram analyzed: Z, vertical; N, north-south; E, east-west. M indicates that the microseism preceding the *P* phase is analyzed.

TABLE 2
LIST OF EARTHQUAKES IN SOUTHWESTERN ASIA, SOUTHEASTERN EUROPE GROUP*

Shock Code	Origin			Time			Coordinates		D (km)	M	Location	Station	Delta (deg)	Azimuth (deg)	Angle of Incidence† (deg)	Later Phase‡ (sec)	T ₁ § (sec)	T ₂ (sec)	Component¶
	y	m	d	h	m	s	Lat. (deg)	Long. (deg)											
NE 17	70	06	05	04	53	06.4	42.5N	78.8E	20	6.0	Atma-ata-Region	FLO	98.5	8.1	19.3	PcP 46	80	40	ZN M
NE 18	67	10	18	01	11	44.8	79.8N	2.4E	33	5.7	Greenland Sea	SHA	60.1	11.9	29.8	PcP 54	80	40	ZN M
												OXF	56.6	12.3	31.1	PcP 71	80	40	ZN
NE 19	63	03	28	00	15	51.4	66.1N	20.1W	33	5.6	Iceland Region	FLO	52.6	13.0	32.4		80	40	ZN
NE 20	66	08	19	12	22	10.7	39.2N	41.6E	33		Turkey	OXF	47.4	31.4	34.4		80	40	ZNE
												FLO	93.8	36.0	19.6		80	40	ZN
												FLO	90.8	35.3	20.1		68	40	ZNE
NE 21	67	07	22	16	56	53.3	40.7N	30.8E	4	6.0	Turkey	MDS	86.8	35.7	20.6		80	40	ZN M
												SHA	89.3	41.7	20.0		80	40	ZNEM
												OXF	87.1	41.1	20.6		80	40	ZNE
NE 22	70	03	28	21	02	23.4	39.2N	29.5E	20	6.0	Turkey	FLO	84.4	40.8	21.5		80	40	ZNE
												SHA	89.5	43.5	20.0		69	40	ZNEM
NE 23	64	10	06	14	31	19.2	40.3N	28.2E	10	6.0	Turkey	OXF	87.4	42.9	20.5		80	40	ZNEM
NE 24	68	02	19	22	45	41.2	39.4N	25.0E	7		Aegean Sea	MDS	79.7	43.4	23.2		80	40	ZEM
												SHA	86.6	45.5	20.7		80	30	ZN M
												OXF	84.7	45.1	21.3		80	30	ZNEM
NE 25	67	03	04	17	58	06.4	39.2N	24.6E	33		Aegean Sea	SHA	86.5	45.9	20.7		80	40	ZN M
												FLO	82.2	45.3	22.3		80	35	ZNEM
NE 26	65	03	31	09	47	30.7	38.6N	22.4E	78	6.3	Greece	OXF	83.7	47.0	21.5	pP 20	74	40	ZNEM
												FLO	81.3	47.0	22.5	sP 30	75	36	ZN M
												MDS	77.9	47.9	23.6		80	40	ZNE
NE 27	65	07	06	03	18	42.7	38.4N	22.4E	20	5.9	Greece	SHA	85.6	47.6	21.0		80	37	ZNE
												OXF	83.8	47.2	21.5		80	40	ZNE
												FLO	81.5	47.1	22.5		80	40	ZNE
												MDS	78.0	48.1	23.8		80	40	ZNE

* Information on these earthquakes is from the Earthquake Data Reports of the USCGS. The symbols are explained in the footnotes to Table 1.

TABLE 3
LIST OF EARTHQUAKES IN SOUTH AMERICA GROUP*

Shock Code	Origin			Time		Coordinates		D (km)	M	Location	Station	Delta (deg)	Azimuth (deg)	Angle of Incidence† (deg)	Later Phase‡ (sec)	T ₁ § (sec)	T ₂ (sec)	Component¶
	y	m	d	h	m	s	Lat. (deg)	Long. (deg)										
SE 28	68	08	23	22	36	51.3	22.0S	63.6W	5.8	Salta Province, Argentina	OXF	61.3	152.5	28.5	PcP 37	80	36	ZN M
SE 29	67	09	09	10	06	44.1	27.7S	63.1W	5.8	Santiago Del. Estero Province, Argentina	SHA	62.8	155.0	27.9	PcP 32	80	32	ZNEM
SE 30	67	02	15	16	11	11.8	9.0S	71.3W	6.2	Peru-Brazil Border Region	OXF	66.7	154.7	26.6	PcP 27	80	40	ZNE
SE 31	65	11	03	01	39	03.1	9.1S	71.4W	5.93	Peru-Brazil Border Region	SHA	70.9	154.5	25.3	PcP 16	80	40	ZNE
SE 32	63	11	09	21	15	30.4	9.0S	71.3W	5.9	Peru-Brazil Border Region	OXF	46.5	155.0	33.2	PcP 80	80	38	ZN M
SE 33	63	08	15	17	25	05.9	13.8S	69.3W	5.43	Peru-Bolivia Border Region	SHA	50.8	155.4	31.4	PcP 66	66	40	ZNEM
SE 34	67	12	27	09	17	55.7	21.2S	68.3W	6.4	Chile-Bolivia Border Region	SHA	42.7	155.2	34.4	PcP 99	80	37	ZN M
SE 35	70	06	11	06	02	54.9	24.5S	68.3W	6.3	Chile-Argentina Border Region	SHA	46.6	155.2	32.9	PcP 80	80	40	ZN M
SE 36	66	05	01	16	22	55.5	8.4S	74.3W	5.8	Peru-Brazil Border Region	SHA	50.8	155.5	31.4	PcP 66	66	40	ZNEM
SE 37	65	09	17	11	13	56.4	1.5S	77.7W	6.2	Ecuador	MDS	50.7	155.6	31.7	PcP 67	67	40	ZNE
SE 38	66	06	07	00	59	46.6	15.0S	75.8W	5.5	Near Coast of Peru	SHA	59.9	156.9	28.9	PcP 40	80	40	ZNE
SE 39	63	09	24	16	30	16.0	10.6S	78.0W	6.0	Near Coast of Peru	OXF	55.0	157.3	31.4	pP 31	30	30	ZN M
SE 40	65	12	15	23	05	22.6	7.5N	82.2W	5.9	South of Panama	SHA	58.9	156.9	30.0	pP 32	30	30	ZN M
SE 41	63	05	19	01	03	06.2	46.3S	74.8W	6.3	Near Coast of Southern Chile	SHA	63.2	156.9	28.8	pP 32	28	28	ZNEM
												58.0	158.8	30.4	pP 27	28	28	ZNE
												66.2	158.2	27.8	pP 27	29	29	ZNE
												49.3	158.8	33.3	pP 34	34	34	ZNE
												53.4	160.8	32.0	pP 34	37	37	ZNE
												33.5	160.9	38.9	pP 40	39	39	ZN M
												37.5	160.5	37.3	pP 41	41	41	ZN M
												55.2	162.8	31.4	PcP 62	80	40	ZNE
												54.8	165.8	31.4	sP 30	80	37	ZNEM
												36.3	167.3	38.4	PP 80	68	40	ZN M
												90.3	169.7	20.1		80	40	ZN

* Information on these earthquakes is from the Earthquake Data Reports of the USCGS. The symbols are explained in the footnotes to Table 1.

DATA PROCESSING FOR THE STUDY OF CRUSTAL STRUCTURE

Assumptions. The following assumptions are made in constructing crustal models.

- (a) Crustal model is assumed to be composed of homogeneous parallel layers, each of which has constant velocities and density.
- (b) *P*-wave velocity models are assumed, which were derived from nearby refraction surveys.
- (c) *S*-wave velocities and densities are assumed to be related to *P*-wave velocities by the relations,

$$\beta = [(1-2\sigma)/(2-2\sigma)]^{\frac{1}{2}}\alpha \quad (1)$$

$$\rho = 2.35 + 0.036(\alpha - 3.0)^2 \quad (2)$$

where Poisson's ratio, σ , is taken as 0.26. The latter relation is composed of the experimental relations of Woollard (1959), and Nafe and Drake (1963).

Possible deviations of the actual structure from the above assumptions will be examined later.

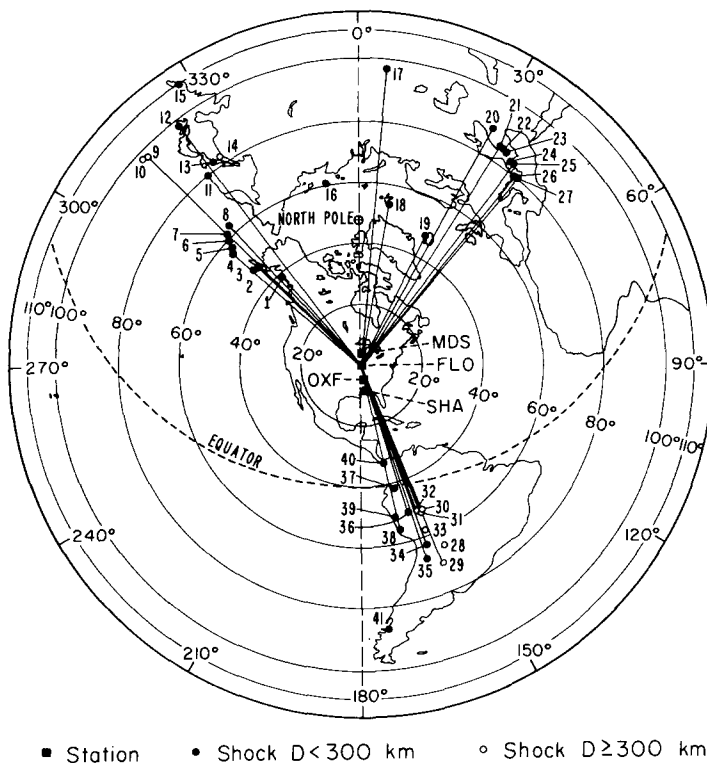


FIG. 1. Geographical distribution of earthquakes relative to four WWSSN stations in the central United States. Solid lines show the propagation paths of body waves to FLO.

Data processing. Previous researches suggest that the crustal thickness in the central United States is about 40 km. For this amount of crustal thickness, a time length of about 40 sec of the teleseismic *P* phase contains most of the information on the crustal layering (Kurita, 1973a). However, even for records of deep earthquakes, this time length is seldom free from later phases, and for those of shallow earthquakes, this time length contains surface and near-surface reflections around the source, bringing troughs into the resultant spectrum. The insensitivity of the transfer ratio to the angle of incidence to the Moho,

makes it possible to superpose observational transfer ratios for earthquakes with different focal depths and almost the same directions of wave approach. This manipulation enables one to locate trough positions and to compose further reliable observational ratios.

By taking the fiducial time at the beginning of the direct P phase, we apply one wing of one or both of the data windows, $w_1(t)$ and $w_2(t)$ to the signal, where

$$w_1(t) = 1/T_1 \cdot [\sin(\pi t/T_1)/(\pi t/T_1)]^2 \quad |t| < T_1 \quad (3)$$

$$w_2(t) = 1/T_2 \cdot [1 - (t/T_2)^2]^0 \quad |t| < T_2 \quad (4)$$

These data windows and an illustration of the signal modification due to their multiplication are shown in Figure 2 with the corresponding spectral windows. T_1 and T_2 , the time length of the above data windows, are taken as 80 and 40 sec, respectively. When no strong later phases are observed within a time length of about 40 sec, $w_2(t)$ applied with

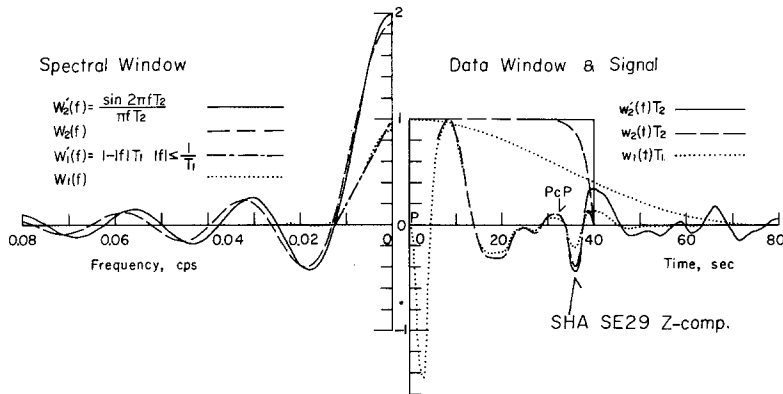


FIG. 2. The *right half* shows one wing of each of the data windows, $w_1(t)$, $w_2(t)$, and $w_2'(t)$ (rectangular window), multiplied by T_1 (80 sec) or T_2 (40 sec), and an illustration of the signal modification due to their application. The vertical component of a P -wave record of a deep earthquake in South America observed at SHA is shown with a solid line, while the signals multiplied by the data windows are shown with the same lines with the data windows. In the *left half* is shown one wing of each of the spectral windows corresponding to the above data windows, and $w_1'(f)$, the Fourier pair of $w_1'(t) = 1/T_1 \cdot [\sin(\pi t/T_1)/(\pi t/T_1)]^2$, $|t| < \infty$.

T_2 of 40 sec best conserves information on the crustal layering of about 40 km. However, some distortions in the resultant spectrum are unavoidable due to the rather large side lobes of the corresponding spectral window. A vertical P -wave record at SHA contains the PcP phase at about 32 sec after the P phase. Since the signal multiplied by $w_2(t)$ with T_2 of 40 sec does not taper the PcP phase and rather distorts the signal, we have taken T_2 as 32 sec as shown in Table 3. $w_2(t)$ is exclusively used when the time length is shortly limited due to a strong later phase. When we can take the time length as long as 80 sec, a multiplication of $w_1(t)$ may bring about the spectrum with sufficient information on the crustal layering. In Figure 2, it is observed that this window nearly succeeds in tapering out the PcP phase. However, we had better not apply this window with a time length as short as 40 sec, because its strong smoothing effect produces a featureless spectrum. Thus, by taking the time length of 80 sec for $w_1(t)$ and 40 sec for $w_2(t)$ as far as possible, and sometimes varying the time length, we calculate observational transfer ratios and obtain a composite for each earthquake. Resultant composites are put together separately for each group. On the other hand, the theoretical transfer ratio is calculated on the assumptions made above. By varying each layer thickness of the assumed velocity models within a probable range, computing transfer ratios, and comparing them with observational ratios, we obtain one or two "best-fit models" in each group for each assumed velocity

model. Thereafter, the best-fit models are rated subjectively in accordance with the quality of fit (see Tables 4, 5, 6 and 7). Among these models "the best models" are selected in each group (see Table 8). All through the above procedure, some objective measure is desirable, but difficult at present.

TABLE 4
CRUSTAL MODELS AROUND SPRING HILL (SHA)

Model	Parameter	Layer						Reference	Quality of Fit*
		1	2	3	4	5	6		
Ansley†	α (km/sec)	3.0	5.1	6.0		6.9	8.3	Fig. 3(d)	D(SE)
Warren, Healy, and Jackson (1966)	ρ (g/cm ³)	2.3	2.6	2.8		3.0	3.3		
	H (km)	4.0	2.0	15.0		20.0	(41.0)		
	α (km/sec)	3.0	4.8	5.9		6.9	8.4	Fig. 3(d)	D(SE)
Raleigh†	ρ (g/cm ³)	2.3	2.6	2.8		3.0	3.3		
	H (km)	3.0	5.0	5.0		16.0	(29.0)		
	α (km/sec)	4.4	4.8	6.0		6.8	8.3	Fig. 3(d)	B(SE)
Dribble† Springer (1966)	β (km/sec)	2.5	2.7	3.6		4.1	4.6		
	ρ (g/cm ³)	2.2	2.3	2.8		3.0	3.4		
	H (km)	3.0	2.5	11.0		20.0	(36.5)		
SHA71-NW	α (km/sec)‡	3.0	5.0	6.0		6.9	8.1	Fig. 3(a)	A
	H (km)	3.0	3.0§	15.0		11.0	(32.0)		
	H (km)	3.0	3.0§	15.0		12.0	(33.0)	Fig. 3(b)	A
NE	H (km)	3.0	3.0§	13.0		16.0	(35.0)	Fig. 3(c)	AA
SE1	H (km)‡	3.0	0.0	16.0		16.0	(35.0)	Fig. 3(d)	AA
SE2	H (km)‡	0.0	3.0	16.0		16.0	(35.0)	Fig. 3(d)	B
SE3	H (km)‡	4.0	2.0	13.0		16.0	(35.0)	Fig. 3(d)	C
SHA71-NW-A	α (km/sec)‡	3.0			6.6		8.15	Fig. 3(a)	B
	H (km)	0.0§			34.0		(34.0)		
	H (km)	0.0§			35.0		(35.0)	Fig. 3(b)	B
NE-A	H (km)	0.0§			37.0		(37.0)	Fig. 3(c)	B
SE-A	H (km)	4.0			33.0		(37.0)	Fig. 3(d)	A

* Rank of fit of the transfer ratio of the model to the observational transfer ratios concerned: AA, excellent; A, good (satisfactory); B, fair; C, poor; D, nonfit. The sector letter in the parentheses shows the sector for which the comparison has been made. When the sector letter is not shown, it means that the rank of fit is the same for three sectors.

† Proposed model.

‡ Parameters are assumed.

§ Assumed value.

|| ± 0.3 km/sec.

TABLE 5
CRUSTAL MODELS AROUND OXFORD (OXF)

Model	Parameter	Layer						Reference	Quality of Fit*
		1	2	3	4	5	6		
Little Rock†	α (km/sec)		4.7	6.2	6.5	7.4	8.1	Fig. 4(d)	D
McCamy and Meyer (1966)	H (km)		6.5	4.5	21.0	14.0	(46.0)		
	H (km)		1.0	5.5	22.5	15.5	(44.5)	Fig. 4(d)	B
Cape Girardeau†	α (km/sec)‡		4.7	6.15	6.5	7.4	8.15	Fig. 4(a)	B
OXF71-NW	H (km)		1.0§	9.0¶	19.0¶	13.0	(42.0)		
	H (km)		1.0§	8.0¶	21.0¶	13.0	(43.0)	Fig. 4(b)	A
NE	H (km)		1.0§	9.0¶	19.0¶	14.0	(43.0)	Fig. 4(c)	B
SE	H (km)		1.0§	9.0¶	19.0¶	4.0	(41.0)	Fig. 4(a)	A
NW1	H (km)		1.0§	9.0¶	27.0¶	4.0	(43.0)	Fig. 4(b)	B
NE1	H (km)		1.0§	9.0¶	29.0¶	4.0	(45.0)	Fig. 4(c)	A
SE1	H (km)		1.0§	9.0¶	31.0¶	4.0	(39.0)	Fig. 4(a)	A
NW2	H (km)		1.0§	9.0¶	29.0¶	0.0§	(40.0)	Fig. 4(b)	B
NE2	H (km)		1.0§	12.0¶	27.0¶	0.0§	(41.0)	Fig. 4(c)	B
SE2	H (km)		1.0§	12.0¶	28.0¶	0.0§	(41.0)	Fig. 4(a)	A
OXF71-NW-A	α (km/sec)‡				6.60		8.15		
	H (km)				39.0		(39.0)		
	H (km)				40.0		(40.0)	Fig. 4(b)	C
NE-A	H (km)				41.0		(41.0)	Fig. 4(c)	C
SE-A	H (km)								
Early Rise (Modified)** Green and Hales (1968)	α (km/sec)			6.3		7.0	8.05	Fig. 6(d)	D
	H (km)			20.0		30.0	(50.0)		
OXF71-NW-B	α (km/sec)‡		4.7	6.3		7.0	8.15	Fig. 4(d)	AA
	H (km)		1.0§	29.0		9.0	(39.0)		
NE-B	H (km)		1.0§	30.0		10.0	(41.0)	Fig. 4(d)	A
SE-B	H (km)		1.0§	32.0		10.0	(43.0)	Fig. 4(d)	AA

Symbols *, †, ‡, §, are explained in the footnotes to Table 4.

¶ The boundary between two layers marked with this symbol in the same row, can be moved by as much as 10 km, with the same or a little worse quality of fit.

** Modified proposed model in which the 6.30 and 7.00 km/sec layers are substituted for the transitional layers of the proposed model, which has a linear increase of the velocity one from 6.30 to 6.35 km/sec over 20 km, and another from 6.85 to 7.15 km/sec over 30 km.

TABLE 6
CRUSTAL MODELS AROUND FLORISSANT (FLO)

Model	Parameter	Layer						Reference	Quality of Fit*
		1	2	3	4	5	6		
5A (Hannibal)†	α (km/sec)	5.0	6.05	6.2	6.6		7.95	Fig. 5(d)	A(NW)
Stewart (1968)	H (km)	1.0	4.0	13.5	20.0		(38.5)		
540312 (Ste. Genevieve)†	α (km/sec)	5.0	6.05	6.25	6.9		8.0	Fig. 5(d)	C(SE)
	H (km)	0.5	3.0	21.5	19.5		(44.5)		
540302 (Ste. Genevieve)†	H (km)	0.5	3.0	36.0			(39.5)	Fig. 5(d)	B(SE)
F1071-NW	α (km/sec)‡	5.0	6.05	6.2	6.6		8.15	Fig. 5(a)	A
	H (km)	1.0§	3.0§	18.0	19.0		(41.0)		
NE	H (km)	1.0§	3.0§	17.0	20.0		(41.0)	Fig. 5(b)	B
SE	α (km/sec)‡	5.0	6.05	6.25	6.9		8.15	Fig. 5(c)	B
	H (km)	1.0§	3.0§	17.0	21.0		(42.0)		
SE1	H (km)	1.0§	3.0§	37.0			(41.0)	Fig. 5(d)	C
Cape Girardeau†	α (km/sec)	4.7		6.2	6.5	7.4	8.1	Fig. 5(d)	C(SE)
McCamy and Meyer (1966)	H (km)	1.0		5.5	22.5	15.5	(44.5)		
FLO71-NW-A	α (km/sec)‡	5.0		6.15	6.5	7.4	8.15	Fig. 5(a)	A
	H (km)	1.0§		9.0¶	27.0¶	9.0	(46.0)		
NE-A	H (km)	1.0§		9.0¶	26.0¶	11.0	(47.0)	Fig. 5(b)	A
SE-A	H (km)	1.0§		9.0¶	26.0¶	12.0	(48.0)	Fig. 5(c)	A
SE-A1	H (km)	1.0§		9.0¶	38.0¶	9.0	(57.0)	Fig. 5(d)	AA
NW-B	α (km/sec)‡	5.0	6.05	6.2	6.6	7.4	8.15	Fig. 5(a)	A
	H (km)	1.0§	3.0§	17.0	16.0	9.0	(46.0)		
NE-B	H (km)	1.0§	3.0§	16.0	16.0	10.0	(46.0)	Fig. 5(b)	A
SE-B	α (km/sec)‡	5.0	6.05	6.25	6.9	7.4	8.15	Fig. 5(c)	AA
	H (km)	1.0§	3.0§	18.0	16.0	14.0	(52.0)		
Central U.S.†	α (km/sec)		6.1	6.4	6.7		8.15	Fig. 5(d)	B(NW)
McEvilly (1964)	β (km/sec)		3.5	3.7	3.95		4.75		C(NE, SE)
	ρ (g/cm ³)		2.7	2.9	2.9		3.3		
	H (km)		11.0	9.0	18.0		(38.0)		
Central U.S. (Modified)	α (km/sec)		6.1	6.4	6.7		8.15	Fig. 5(d)	C(SE)
	H (km)		11.0	9.0	18.0		(38.0)		
FLO (Two Layer)†	α (km/sec)			6.2	6.6		8.2	not shown	A(NW) B(NE, SE)
Fernandez and Careage (1968)	H (km)			21.0	21.0		(42.0)		
FLO (One Layer)†	α (km/sec)				6.5		8.2	not shown	A(NW) B(NE, SE)
	H (km)				43.0		(43.0)		
FLO71-NW-C	α (km/sec)‡				6.6		8.15	Fig. 5(a)	A
	H (km)				42.0		(42.0)		
NE-C	H (km)				43.0		(43.0)	Fig. 5(b)	B
SE-C	H (km)				44.0		(44.0)	Fig. 5(c)	C
Early Rise (Modified)**	α (km/sec)			6.3		7.0	8.05	Fig. 5(d)	D
Green and Hales (1968)	H (km)			20.0		30.0	(50.0)		
FLO71-NW-D	α (km/sec)	5.0		6.3		7.0	8.15	Fig. 5(e)	A
	H (km)	1.0§		20.0		20.0	(41.0)		
NW-D1	H (km)	1.0§		33.0		8.0	(42.0)	Fig. 5(e)	A
NE-D	H (km)	1.0§		34.0		8.0	(43.0)	Fig. 5(e)	A
SE-D	H (km)	1.0§		22.0		30.0	(53.0)	Fig. 5(e)	AA
SE-D1	H (km)	1.0§		37.0		14.0	(52.0)	Fig. 5(e)	A

For explanation of symbols, see footnotes to Tables 4 and 5.

TABLE 7
CRUSTAL MODELS AROUND MADISON (MDS)

Model	Parameter	Layer					Reference	Quality of Fit*
		2	3	4	5	6		
913A (SE End)† Steinhart and Meyer (1961)	α (km/sec)	5.4	6.1	6.5		8.0	Fig. 6(d)	B
913B (SE End)†	H (km)	1.0	11.5	25.0		(37.5)		
	α (km/sec)	5.4	6.3			8.1	Fig. 6(d)	C
MDS71-NW	H (km)	3.0	32.0			(35.0)		
	α (km/sec)‡	5.4	6.1	6.5		8.15	Fig. 6(a)	A
NE	H (km)	2.0§	11.0¶	27.0¶		(40.0)		
	H (km)	2.0§	11.0¶	26.0¶		(39.0)	Fig. 6(b)	A
SE	H (km)	2.0§	11.0¶	26.0¶		(39.0)	Fig. 6(c)	A
NW1	α (km/sec)‡	5.4		6.3		8.15	Fig. 6(a)	A
NE1	H (km)	2.0§		38.0		(40.0)		
	H (km)	2.0§		37.0		(39.0)	Fig. 6(b)	A
SE1	H (km)	2.0§		37.0		(39.0)	Fig. 6(c)	A
Early Rise (Modified)**	α (km/sec)		6.3		7.0	8.05	Fig. 6(d)	D
Green and Hales (1968)	H (km)		20.0		30.0	(50.0)		
MDS71-NW-A	α (km/sec)‡	5.4	6.3		7.0	8.15	Fig. 6(a)	AA
NE-A	H (km)	2.0§	28.0		11.0	(41.0)		
	H (km)	2.0§	28.0		10.0	(40.0)	Fig. 6(b)	AA
SE-A	H (km)	2.0§	30.0		9.0	(41.0)	Fig. 6(c)	AA
SE-A1	α (km/sec)‡	5.4	6.1	6.5	7.0	8.15	Fig. 6(d)	A
MDS71-NW-B	H (km)	2.0§	11.0	19.0	9.0	(41.0)		
	α (km/sec)‡			6.6		8.15	Fig. 6(a)	A
NE-B	H (km)			41.0		(41.0)		
	H (km)			40.0		(40.0)	Fig. 6(b)	A
SE-B	H (km)			40.0		(40.0)	Fig. 6(c)	A

For explanation of symbols, see footnotes to Tables 4 and 5.

TABLE 8
THE BEST CRUSTAL MODELS AROUND SHA, OXF, FLO, AND MDS

Model	Parameter	Layer						Reference	Quality of Fit*
		1	2	3	4	5	6		
SHA71-NW	α (km/sec)‡	3.0	5.0	6.0		6.9	8.1	Fig. 3(a)	A
	β (km/sec)	1.71	2.85	3.42		3.93	4.61		
	ρ (g/cm ³)	2.35	2.5	2.65		2.9	3.3		
	H (km)	3.0	3.0§	15.0		11.0	(32.0)		
NE	H (km)	3.0	3.0§	15.0		12.0	(33.0)	Fig. 3(b)	A
	H (km)	3.0	3.0§	13.0		16.0	(35.0)	Fig. 3(c)	AA
OXF71-NW-B	α (km/sec)‡		4.7	6.3		7.0	8.15	Fig. 4(d)	AA
	β (km/sec)		2.7	3.59		3.99	4.64		
	ρ (g/cm ³)		2.45	2.75		2.95	3.3		
	H (km)		1.0§	29.0		9.0	(39.0)		
NE-B	H (km)		1.0§	30.0		10.0	(41.0)	Fig. 4(d)	A
	H (km)		1.0§	32.0		10.0	(43.0)	Fig. 4(d)	AA
FLO71-NW-A	α (km/sec)‡		5.0	6.15	6.5	7.4	8.15	Fig. 5(a)	A
	β (km/sec)		2.85	3.5	3.7	4.21	4.64		
	ρ (g/cm ³)		2.5	2.7	2.8	3.05	3.3		
	H (km)		1.0§	9.0¶	27.0¶	9.0	(46.0)		
NE-A	H (km)		1.0§	9.0¶	26.0¶	11.0	(47.0)	Fig. 5(b)	A
	H (km)		1.0§	9.0¶	38.0¶	9.0	(57.0)	Fig. 5(d)	AA
MDS71-NW-A	α (km/sec)‡		5.4	6.3		7.0	8.15	Fig. 6(a)	AA
	β (km/sec)		3.07	3.59		3.99	4.64		
	ρ (g/cm ³)		2.55	2.75		2.95	3.3		
	H (km)		2.0§	28.0		11.0	(41.0)		
NE-A	H (km)		2.0§	28.0		10.0	(40.0)	Fig. 6(b)	AA
SE-A	H (km)		2.0§	30.0		9.0	(41.0)	Fig. 6(c)	AA

For explanation of symbols, see footnotes to Tables 4 and 5.

CRUSTAL STRUCTURE FROM *P*-WAVE SPECTRA

Besides the terms, the best-fit model and the best model defined above, we give working definitions for the terms whose meaning is more or less ambiguous. According to James and Steinhart (1966), we define "the crust" as the outer shell of the Earth lying above the level at which the *P*-wave velocity increases rapidly or discontinuously to values in excess of 7.6 km/sec. When referring the area studied to the geological provinces, such as "the Gulf coastal plain", "the interior plain", and "the superior upland", we refer to Figure 2 of Pakiser and Robinson (1966).

Spring Hill (SHA). SHA is situated at the southern end of the Gulf coastal plain, facing Mobile Bay. The only refraction profile near SHA runs in a north-south direction about 140 km west of SHA. Table 4 includes model Ansley, the south end, model Raleigh, the north end of the profile, proposed by Warren, Healy, and Jackson (1966), and model Dribble, the shot point model of the SALMON event of Springer (1966). An assumed *P*-wave velocity model is a composite of these models with the velocity in the uppermost mantle of 8.10 km/sec after Herrin (1969). The resultant best-fit models, NW, NE, and SE are shown in Table 4. β and/or ρ , not shown in the table, are calculated from relations (1) and (2). The transfer ratios of the above models are compared with the observational ratios in Figure 3. The small figures included are referred to alphabetically from top to bottom. The thin curves with shock numbers in Figures 3(a), (b), and (c) show observational transfer ratios. The dotted parts of the curves correspond to the frequency ranges where the signal-to-noise ratio is lower than one-half, or where sufficient reliability of the transfer ratio cannot be expected due to the effects of later phases or reflections around the source. The similarities in the features of the curves, especially the spacing of three peaks within each group and among three groups, imply that the crustal structure around this station may be primarily approximated by horizontal parallel layering. Generally, the lowest-frequency peak (the first peak) is less reliable than the peak next to it (the second peak). This is experimentally substantiated by the fact that the first peak is usually lower in amplitude and that its position is generally more sensitive to various factors such as differences in data window and time length of analysis. Therefore, the matching of the second peak is considered to be the most important. A satisfactory fit is attained in three sectors. Some discrepancies of the observational ratios among three sectors have resulted in some differences in each layer and total crustal thicknesses.

Next, based on a unilayered velocity model shown in Table 4, models, NW-A, NE-A, and SE-A are obtained. These models almost attain the matching of the peak positions, but discrepancies in the relative height of the peaks are noticeable. These discrepancies, however, can largely be reconciled by an introduction of a low-velocity surface layer. This is apparent from a comparison of the transfer ratio of model SE-A1 with the 3.0-km/sec surface layer of 4-km thickness in Figure 3(d), with the observational ratios in Figure 3(c). A comparison of the transfer ratios of models, SE, SE1, SE2, and SE3 in Figures 3(c) and (d), shows that variations in thickness of the 3.0-km/sec layer have a noticeable effect on the transfer ratios as compared with the negligible effect of the 5.0-km/sec layer, and that the thickness of the 3.0-km/sec layer can be unambiguously determined, especially from the phase difference.

Oxford (OXF). OXF is located about 100 km east of the Mississippi River near an intersection of the Gulf coastal plain and the interior plain. The Arkansas profile runs northeast from Little Rock about 250 km west of OXF. The models at Little Rock, the southwest end, and at Cape Girardeau, the northeast end of the profile, as proposed by McCamy and Meyer (1966) are shown in Table 5. An assumed *P*-wave velocity model is mainly based on the above velocity model. The observational ratios at this station, shown in Figure 4, show a narrower spacing of four peaks, as compared with a wider spacing of three peaks for those at SHA. This may imply an underlying thicker crust. The consistency of the observational ratios within each group and among three groups, may suggest that the layering is approximately horizontal and parallel. The resultant models are composed of three groups of models in which the 7.4-km/sec layer is either thick, thin, or missing. The thickness of the 4.7-km/sec layer is arbitrarily assumed as 1 km, because we have no certain information on it. An increase in thickness of this layer to several kilometers serves only to heighten the fourth peak. For the SE group which contain reliable observational ratios of deep earthquakes, model SE1 is preferred to models SE and SE2

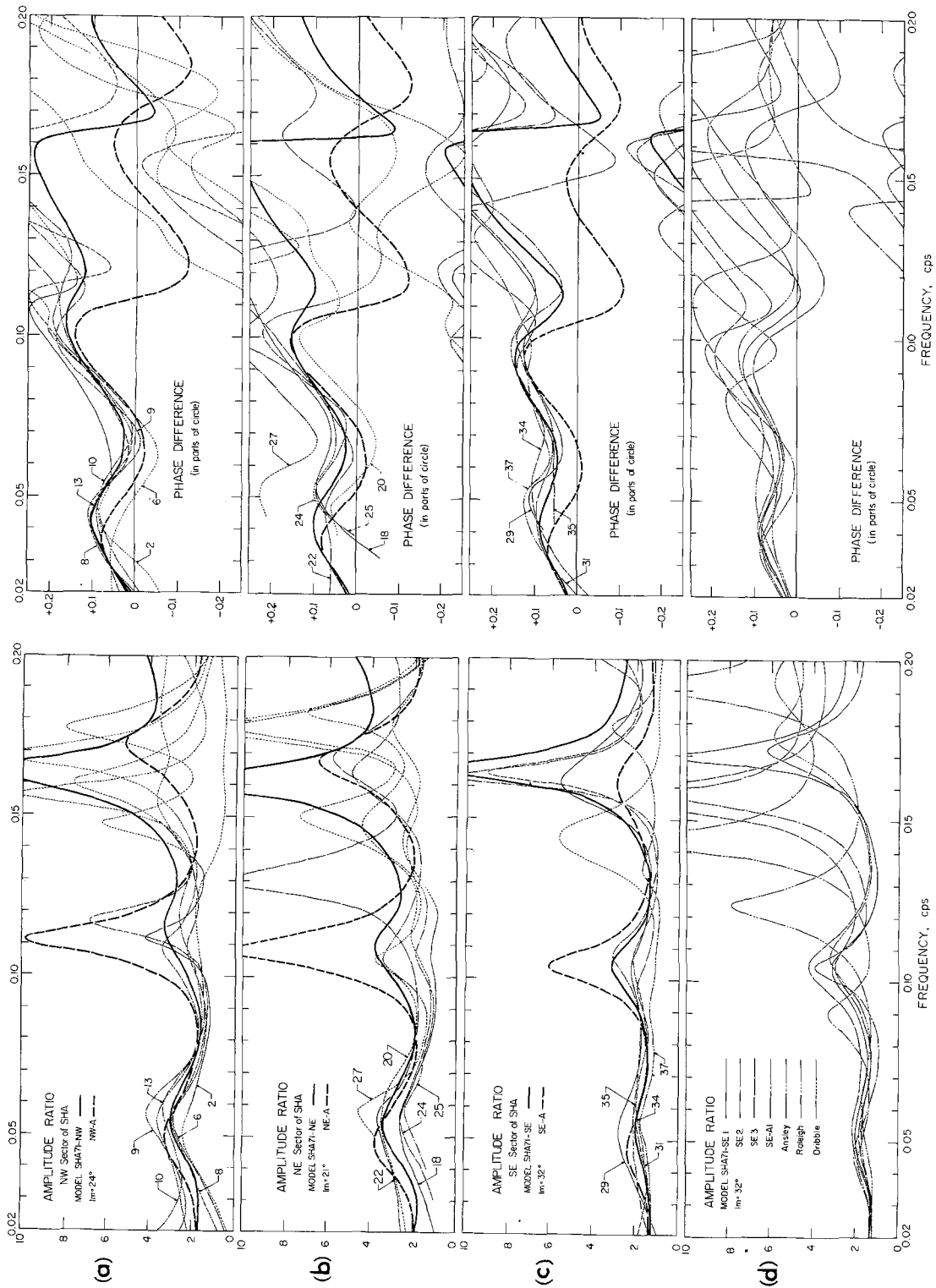


Fig. 3. Comparisons of the transfer ratios of crustal models around SHA in Table 4, with the relevant observational transfer ratios.

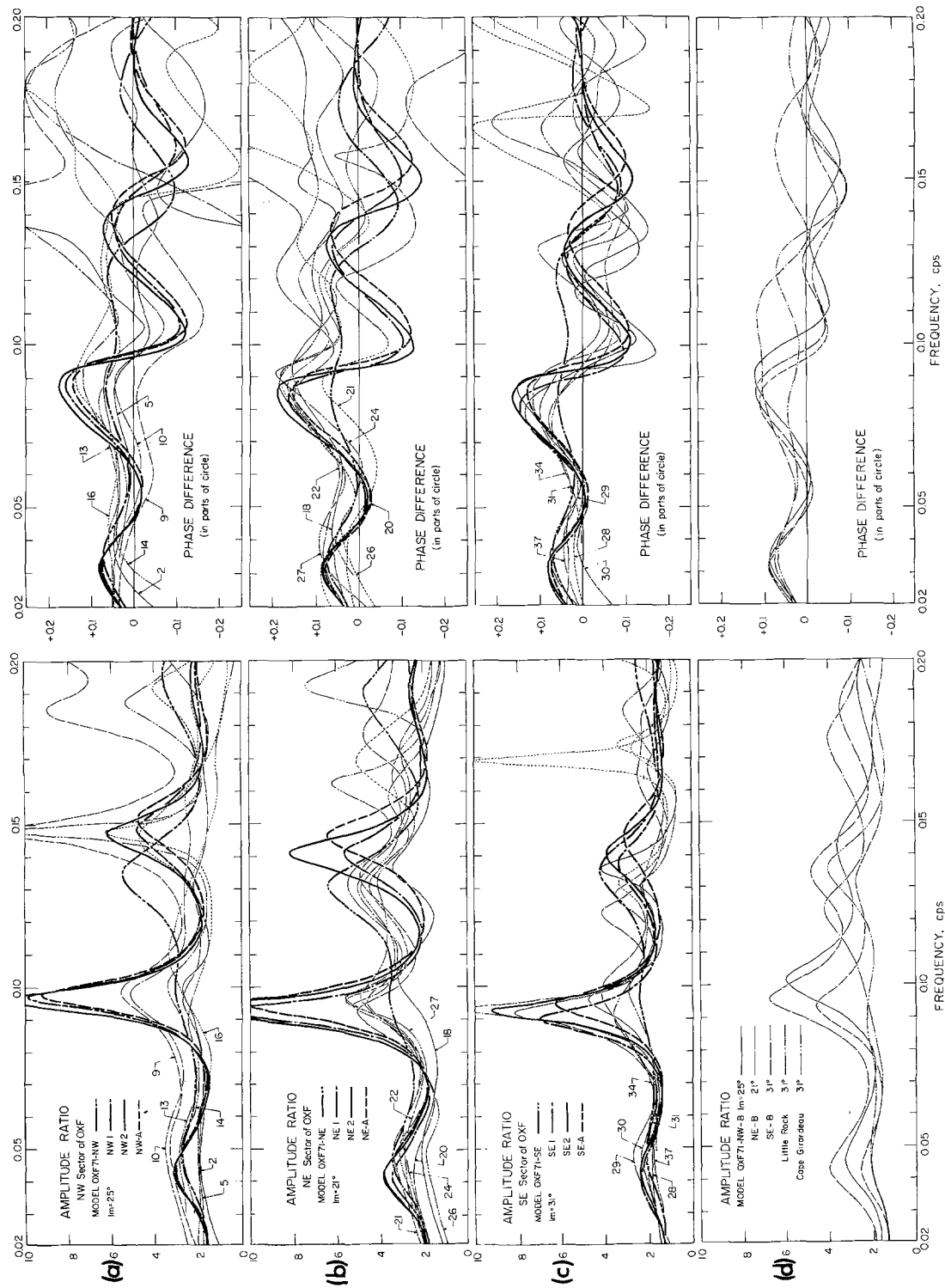


Fig. 4. Comparisons of the transfer ratios of crustal models around OXF in Table 5, with the relevant observational transfer ratios.

because of the better fitting of the relative heights of the peaks. But for the other two groups, this is not the case. Table 5 contains also the best unlayered models in each sector.

The Little Rock profile of Project Early Rise passes about 200 km west of OXF. Green and Hales (1966) made a travel-time study for the Little Rock and Wichita profiles and proposed a model shown in Table 5. A comparison of the transfer ratio of this model in Figure 6(d) with the observational ratios in Figure 4(c) shows that the crustal thickness, as much as 50 km, is too thick to attain a satisfactory fit. An assumed *P*-wave velocity model is based mainly on the above proposed model. The transfer ratios of the inferred models, NW-B, NE-B, and SE-B shown in Figure 4(d), succeed in raising the fourth peak and depressing the second peak and thereby attain a much better fit than those of the other models.

Florissant (FLO). FLO is situated in the midst of the interior plain, and the area surrounding this station has been an object of extensive studies of crustal structure, as apparent from Table 1 of McEvilly (1964). However, the structures estimated by various investigators are not consistent. This may imply the complex structure there. Indeed, although most of the records analyzed are of the earthquakes common to most of the stations, only the observational ratios at FLO, especially the amplitude ratios, show a marked inconsistency in each group and among three groups, as is apparent from Figure 5. Peaks of the observational ratios in the SE group are generally lower than those for the other groups and for the other stations. In addition, the second peak splits into two closely spaced peaks when the window length, T_2 is increased from 30 to 40 sec. Although this splitting is not observed for the other two groups, we regard two closely spaced peaks as more reliable, because 30 sec cannot include the latter part of the reverberations in the crustal layering and its resolution is intrinsically lower.

From a detailed study of two reversed refraction surveys made in Missouri, Stewart (1968) concluded that the crust in northern Missouri may be characterized by three major layers of 6.1, 6.2, and 6.6 km/sec with an underlying upper mantle of 8.0 km/sec, but that the crust in southern Missouri is so laterally inhomogeneous that it cannot be approximated by any simply layered structure. The northern Missouri profile passes in a westerly direction from Hannibal at about 130 km northwest of FLO, while the southern Missouri profile runs toward the southwest from Ste. Genevieve at about 100 km southeast of FLO. For the NE and NW sectors, we assume a velocity model composed primarily of the northern Missouri model of Stewart (1968), except for the velocity in the uppermost mantle of 8.15 km/sec according to Herrin (1969). For the SE sector, assumed velocity models are composed mainly of two models, one with and one without a 6.9-km/sec layer, proposed by Stewart (1968) for southern Missouri. The proposed models for the end of both profiles near FLO and the resultant models are shown in Table 6. The transfer ratios of these models are compared with the observational ratios in Figure 5. Only in the NW sector is a satisfactory fit attained.

We next assume a velocity model composed mainly of the model proposed by McCamy and Meyer (1966) for the Arkansas profile. Cape Girardeau, the northeast end of this profile is situated about 180 km southeast of FLO. The inferred models attain a satisfactory fit for all three sectors. For the SE sector, two models, SE-A and SE-A1 are obtained, depending on whether the splitting of the second peak is taken into account or not. Although the latter model is preferred, as presented in the above discussion, the crustal thickness of this model is slightly too thick for the adopted time length. However, since a slightly longer time length does not bring about a substantial change in observational ratios, we may regard this model as nearly correct, and will settle this problem in Kurita (1973b). Models, NW-A, NE-A, and SE-A1 are preferred to models, NW, NE, and SE. Based on a composite of the above two assumed velocity models, we have obtained models, NW-B, NE-B, and SE-B, which give excellent or satisfactory fit. A

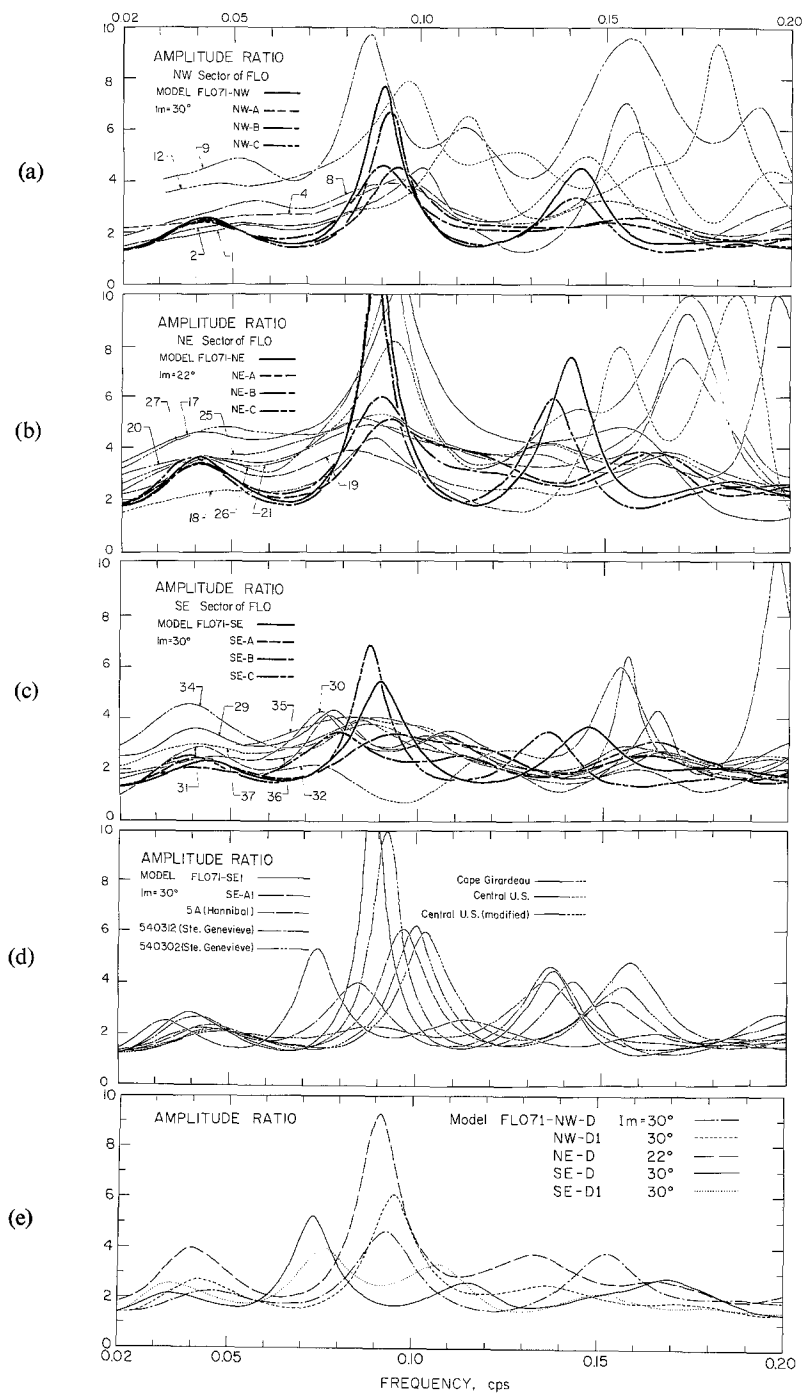


FIG. 5.1.
FIG. 5. Comparisons of the transfer ratios of crustal models around FLO in Table 6, with the relevant observational transfer ratios.

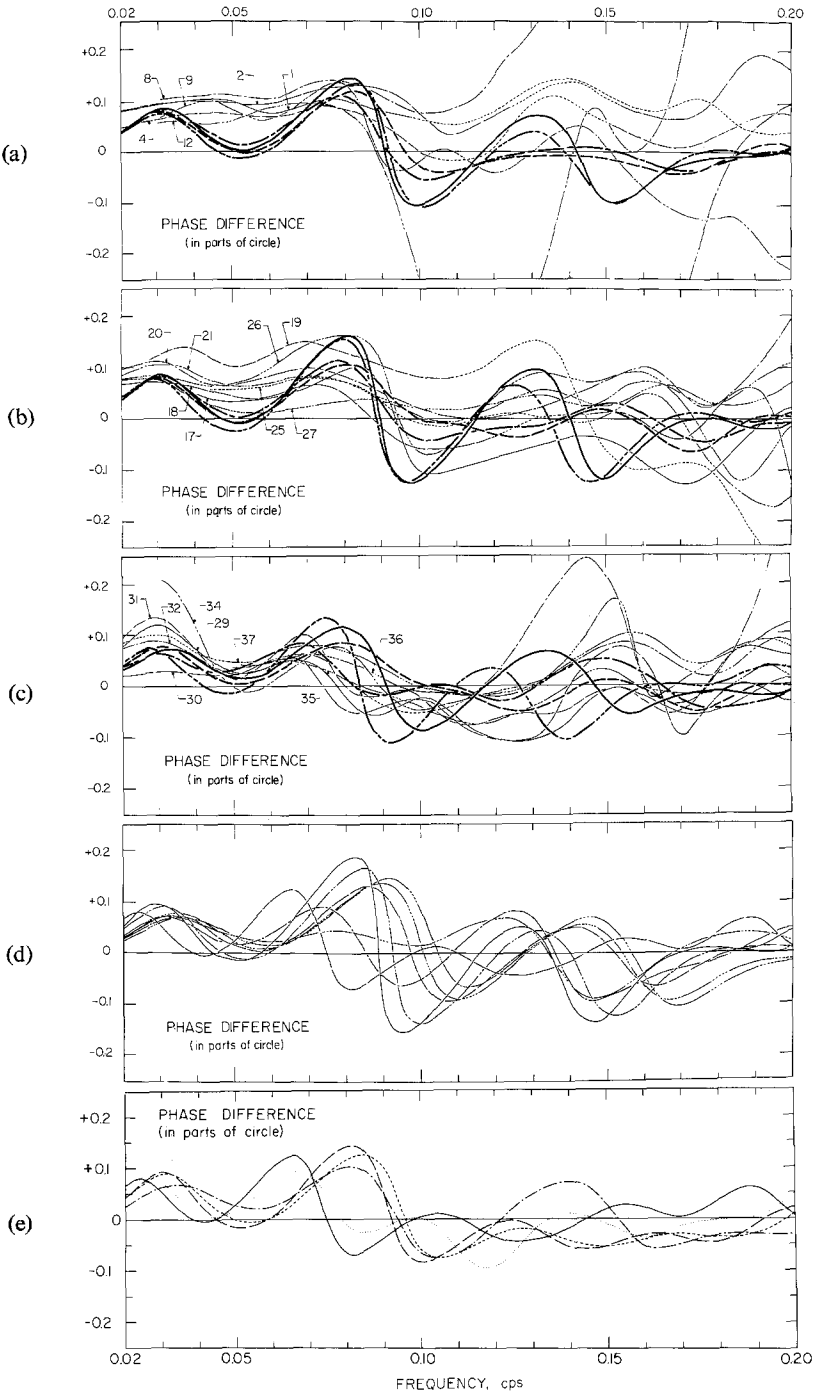


FIG. 5.2.

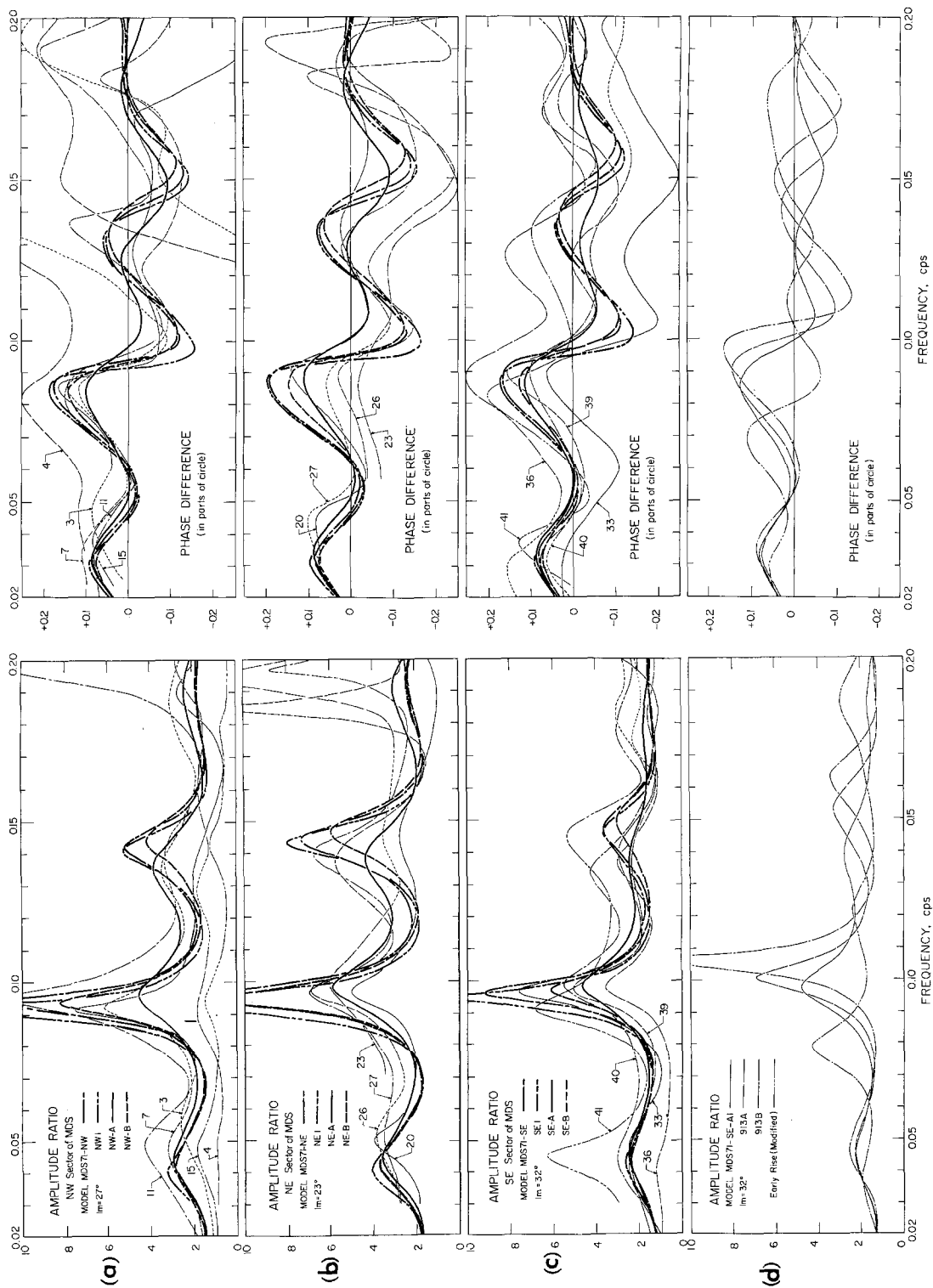


FIG. 6. Comparisons of the transfer ratios of crustal models around MDS in Table 7, with the relevant observational transfer ratios.

discrimination of these models from models, NW-A, NE-A, and SE-A1 is impossible. At present, we prefer the latter models to avoid any artificiality.

Table 6 contains the central U.S. model of McEvelly (1964) obtained from a study of phase-velocity dispersion. This model does not attain a satisfactory fit mainly due to its thinner crustal thickness of 38 km. In the modified central U.S. model, S-wave velocities and densities calculated with relations (1) and (2) are adopted. The difference in transfer ratio of both models is slight, as apparent from Figure 5(d). This table also includes the one- and two-layer models proposed by Fernandez and Careage (1968) for the crust around FLO, from a study of *P*-wave amplitude spectra of a deep earthquake, and the best unilayered models for each sector.

Finally, we assume a velocity model based mainly on the Early Rise model of Green and Hales (1968). The Little Rock profile passes about 50 km west of FLO. The transfer ratios of these models shown in Figure 5(e), fit well with the observational ratios in Figures 5(a), (b), and (c). Taking into account the consistency of layer configuration for three sectors, we can divide these models into two groups, NW-D1, NE-D, and SE-D1,

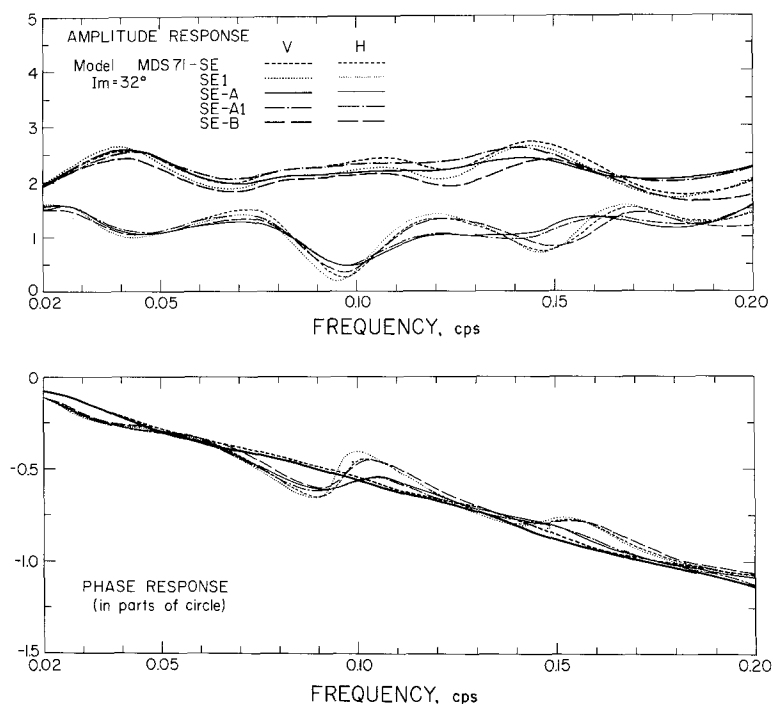


FIG. 7. Comparisons of the vertical (V) and horizontal (H) components of the transfer functions (amplitude and phase responses) of *P* wave of unit amplitude incident at the bottom of the crustal models obtained for the SE sector of MDS. The wave is incident with an angle of 32° and a zero phase shift. For the vertical component of phase response, the response curves are shown for only two models, SE and SE-A, because models, SE1 and SE-B, and model SE-A1 show nearly the same feature as model SE, and model SE-A, respectively.

and NW-D and SE-D. We may be able to find a model with a fair fit for the NE sector of the latter group, but we prefer the former group, although further evidence is needed to substantiate this selection. We may prefer models, NW-A, NE-A, and SE-A1 to models, NW-D1, NE-D, and SE-D1 because of the excellent fit of model SE-A1 as compared with a satisfactory fit for model SE-D1, although again further evidence is desirable.

Madison (MDS). MDS is located near an intersection of the interior plain and the superior upland. It is about 340 km south of Lake Superior, where detailed refraction studies such as Smith, Steinhart, and Aldrich (1966), elucidated the complex crustal

structure. Since this station was closed during December, 1966, a sufficient amount of data cannot be expected, and most of the records analyzed are of shallow earthquakes. Nevertheless, the observational ratios are quite consistent in each group and among three groups, and show nearly the same features as those for OXF.

According to a compilation of McConnell, Gupta, and Wilson (1966), the refraction profile 913 shown in Figure 8 as the Wisconsin profile which extends from about 90 km northeast of MDS nearly to the northwest, is the only reversed survey near MDS. Assumed velocity models are based mainly on two models, 913A and 913B, proposed by Steinhart and Meyer (1961) for the SE end of this profile. The proposed and inferred models are shown in Table 7, and their transfer ratios are compared with the observational ones in Figure 6. Models, NW, NE, and SE and models, NW1, NE1, and SE1 based on the two velocity models give equally satisfactory fit.

Next, we assume a *P*-wave velocity model based on the Early Rise model of Green and Hales (1966). The Little Rock profile passes only about 20 km west of MDS. The transfer ratios of inferred models, NW-A, NE-A, and SE-A succeed in raising the fourth peak and depressing the second peak, which results in a better fit than the transfer ratios of models, NW1, NE1, and SE1, without the 7.0-km/sec layer. The transfer ratio of model SE-A1 in Figure 6(d) shows that division of the 6.3-km/sec layer into the 6.1- and 6.5-km/sec layers produces almost the same, just a slightly worse, fit.

The best unilayered models, NW-B, NE-B, and SE-B, also can give satisfactory fit and have crusts only 1 km thicker than models, NW1, NE1, and SE1. Taking into account the crustal velocity difference of 0.3 km/sec between both groups of models and a negligible effect of the 5.4-km/sec layer on the transfer ratio, this fact shows difficulty in estimating the velocity structure by this method within the frequency range concerned. Eventually, models, NW-A, NE-A, and SE-A are selected as the best models. However, the other models with satisfactory fit in Table 7, may possibly be substituted for the best models. This is apparent from Figure 7, which compares the amplitude and phase responses of all resultant models for the SE sector. Except for some discrepancies for frequencies higher than 0.10 Hz between models, SE-A and SE-A1, and the other models, the response spectra show almost the same features. In this situation, by assuming either of the above models, we may approximately eliminate the crustal effect from observed spectra, at least for the vertical motion.

DISCUSSION

Three sectors around each station, as shown in Figure 8, may be considered as the approximate regions with which the inferred crustal models are concerned. The width of each sector is mostly based on the direction of wave approach from earthquakes shown in Figure 1, while the stretch from the station to the end of the sector is taken as two parts in three of the approximate horizontal distance between the station and the position of the *P* coda which is incident at the station 40 sec later than the direct *P* waves after reverberations in the lower crustal layer of the best models shown in Table 8. As for FLO, we may possibly replace the tabulated models by models derived from the Early Rise velocity model in Table 6. For the NW sector of FLO, model FLO71-NW also cannot be ruled out. Table 9 shows the estimated crustal thickness for the best models and the best unilayered models whose velocities are assumed common to all stations. The crustal thickness of both groups differs at most 10 per cent, but shows almost the same regional variations. It also appears that a thicker crust is concerned with a higher average velocity in the crust. If we take possible alternative models for FLO, the crustal thickness of the NW and NE sectors reduces to about 42 km. In any case, the general trend of the depth

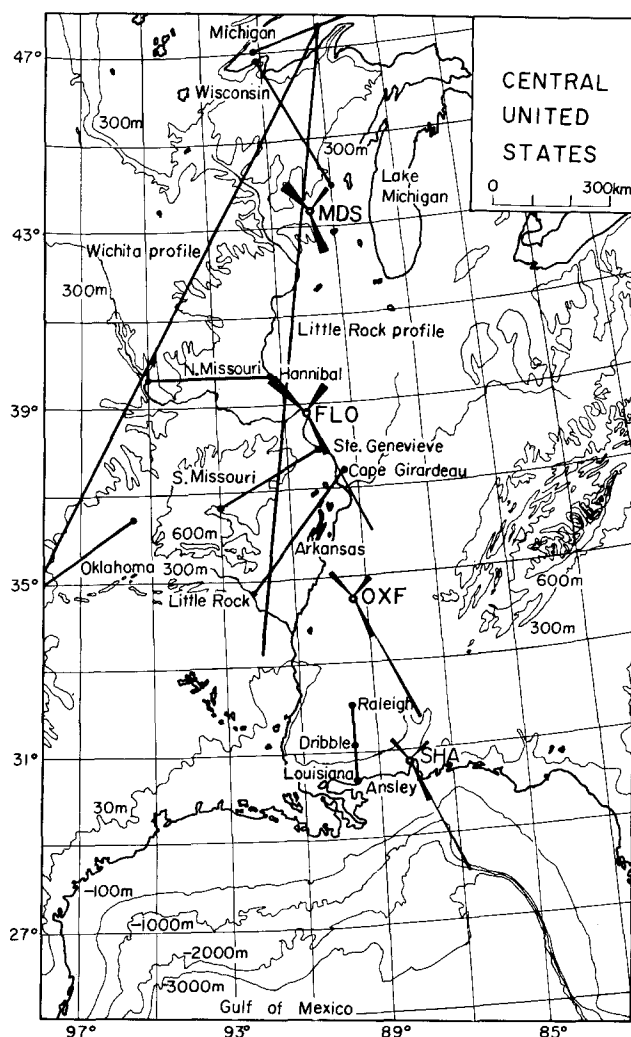


FIG. 8. Map of the central United States. Three sectors enclosing each station nearly correspond to the areas where the crustal structure has been investigated. A long sector extending from the station nearly to the southeast is concerned with the upper mantle structure studied in Kurita (1973b). Solid lines show profiles of major refraction surveys made in this region.

TABLE 9

ESTIMATED CRUSTAL THICKNESSES IN KILOMETERS FOR THE BEST MODELS SHOWN IN TABLE 8, AND UNILAYERED MODELS WHOSE *P*-WAVE VELOCITIES IN THE CRUST AND UPPER MANTLE ARE 6.60 AND 8.15 KM/SEC, RESPECTIVELY

Sector	Best Model (Stations)				Unilayered Model (Stations)			
	SHA	OXF	FLO	MDS	SHA	OXF	FLO	MDS
NW	32	39	46	41	34	39	42	41
NE	33	41	47	40	35	40	43	40
SE	35	43	57*	41	37	41	44	40
Average	33	41	47	41	35	40	43	40

* Value omitted in averaging.

of the Moho may match well with the topographic feature from the Gulf of Mexico to Lake Superior.

Progressive crustal thickening of a few kilometers from the NW, NE, to SE sectors, except for the crust around MDS, is observed in both groups of the models in Table 9. To our regret, however, we are not certain of this result. Since we have utilized the records of shallow earthquakes to examine regional variations in crustal structure around the station,

there is a possibility that a consistent bias of the records of the earthquakes among three sectors has resulted in a systematic shift of peak positions of observational ratios and, accordingly, a systematic discrepancy in crustal thickness. In relation to this fact, the probable error of the total crustal thickness may be no more than a few kilometers for an assumed velocity structure. For the probable error of each layer thickness, we may assign almost the same thickness except for the assumed thickness of the 4.7- to 5.4-km/sec layer and a pair of the layers for which the mutual transfer of their thicknesses is possible by as much as 10 km (see Tables 5, 6, and 7).

An interesting feature concerning the resultant velocity structure is that among assumed *P*-wave velocity models, the Early Rise model has brought about the best models for OXF and MDS, and possibly for FLO, although a marked discrepancy in crustal thickness as much as 10 km is observed between the proposed model and most of the inferred models. This may be mainly due to the fact that their model represents an average feature over the whole region covered by two profiles. We note that the crustal thickness of 50 km of their model nearly coincides with 51 km estimated by Tryggvason and Qualls (1967) and is not far from 46.5 km obtained by Mitchell and Landisman (1971), for the crust in Oklahoma. Since the Early Rise model is not concerned with the southern part of the profiles, the horizontal extrapolation of this velocity model to the structure around OXF may be inappropriate. However, the observational ratios at OXF show almost the same feature as those at MDS where the Early Rise velocity model is well applied, and the transfer ratios of the best models at OXF fit pretty well with the observational ratios there. Accordingly, these models may be regarded as nearly appropriate to the structure around OXF. For the other stations, the horizontal extrapolation is within 200 km. This amount of extrapolation may be permissible, unless there are some unfavorable situations.

The most impressive fact concerning the best models is that they are composed of layers with common features. Except for an additional 3.0-km/sec layer at SHA, this is apparent from an inspection of the parameters in the same row of Table 8. Especially the best models at OXF and MDS show similar features. An apparent inconsistency of the observational ratios at FLO has resulted in a marked discrepancy in layer configuration of the models between the NW and NE sectors and the SE sector. We are certain of the complicated structure around FLO, but not certain whether or not the difference in structure between two groups of the sectors is just the same as shown in Table 8. We require further data, especially some good records of deep earthquakes in the Kurile-Japan region to settle this problem. Figure 12 of Christensen (1965) depicts a relation between rock composition and *P*-wave velocity. The velocity in the upper crust from 6.1 to 6.5 km/sec is appropriate for silicic rock, ranging in composition from granite to diorite, with an average composition close to granodiorite or their metamorphic equivalents, whereas the velocity in the lower crust from 6.9 to 7.0 km/sec is appropriate for mafic rock with a composition close to gabbro or its metamorphic equivalent. Some inclusion of altered ultramafic rocks may be expected for a probable 7.4-km/sec layer around FLO. The velocity in the uppermost mantle of 8.10 to 8.15 km/sec is suitable for ultramafic rock with a composition of predominant peridotite. Pakiser and Robinson (1966), based on results of previous refraction surveys, concluded that the crustal thickness in the United States is predominantly controlled by the thickness of mafic rock in the lower crust. Although the scope of the region in discussion is different, our results indicate the reverse situation that variations in crustal thickness are primarily dominated by silicic upper crust. This is consistent with a finding of Mitchell and Landisman (1971) from a study of refraction surveys in Oklahoma and eastern New Mexico, that the upper 15 to 20 km of the crustal layers controls the difference in crustal thickness. Further discussions on rock composition and related problems are difficult without further data.

Departures from a plane-layered configuration and anelastic or anisotropic properties of the crust, may have some effects on the transfer ratio. However, a conventional amount of anelasticity in the crust has only a negligible effect (Kurita, 1970), whereas anisotropy, if it exists, may be small (Kurita, 1973d), and, accordingly, its effect may be neglected. As for the structural complexity, we limit our discussion to dipping and transitional layer boundaries. Transitional boundary generally lowers the height of peaks of the transfer ratio (Kurita, 1969). A dipping layer interface has the same effect for waves propagating in the down-dip direction, while the situation reverses for waves in the up-dip direction (Ishii and Ellis, 1970). However, an inclination of layer interface within about 10° has a negligible effect for the lower frequencies concerned. A problem somewhat related to the inclination of the layer interface is a possible deviation of the real direction of wave approach from the geometrical azimuth. The effect of this deviation is also small (Kurita, 1973b).

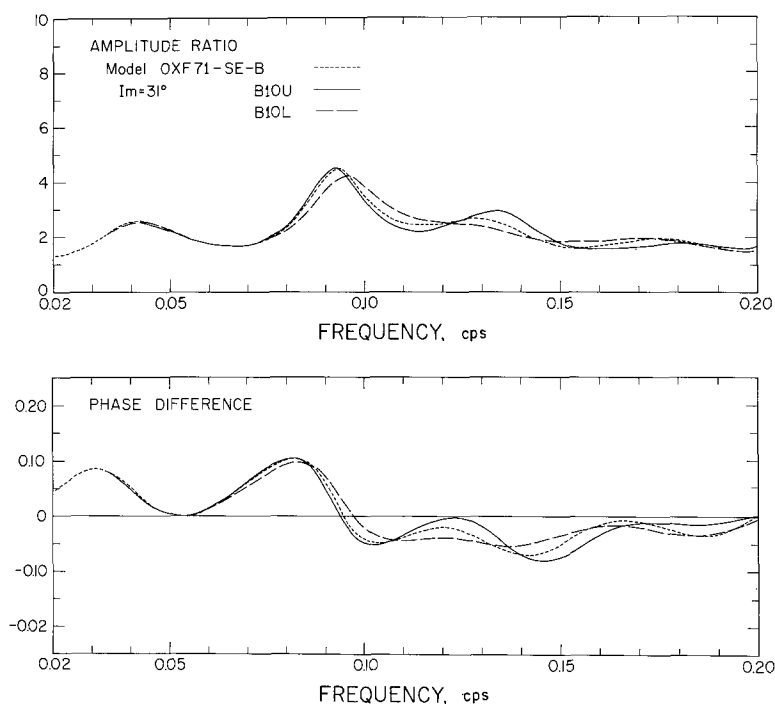


FIG. 9. Comparison of the transfer ratio of model OXF71-SE-B, with those of models, SE-B10U and SE-B10L in which the upper and lower boundaries of the mafic layer of model OXF71-SE-B are replaced by a transitional layer of 10-km thickness, respectively.

Our method is not sensitive enough to detect a small velocity gradient such as about $0.010 \text{ km sec}^{-1} \text{ km}^{-1}$ in the silicic layer in and around the interior plain obtained by Green and Hales (1968) from a travel-time study of Project Early Rise, and $0.005 \text{ km sec}^{-1} \text{ km}^{-1}$ in the silicic layer around FLO suggested by Hill (1971) from a study on amplitude decay of head waves. The following discussion is concerned with the possible existence of more prominent gradual velocity variations with depth, which are sometimes possible as an interpretation of data of refraction surveys, as discussed by McCamy and Meyer (1966). As an interpretation of the layered structure of the inferred models, the thin layer interleaved such as the 5th layer of models, OXF71-NW1, NE1, and SE1 in Table 5, or two adjacent layers for which the velocity difference is small such as the second and third layers of models, FLO71-NW, NE, SE, and SE1 in Table 6, may be regarded as

implications of the transitional nature of the layer interface. Examination of the extent to which the transitional layering is likely at layer interfaces, is possible only for the SE sector of SHA, OXF, and FLO, where the height of peaks of observational ratios of deep earthquakes is rather reliable. As apparent from Figures 3, 4, and 5, the transfer ratios of the inferred models, especially of the best models in Table 8, give almost the same general feature as their corresponding observational ratios, including the height of peaks. Although the model composed of constant-velocity layers is almost certainly an oversimplification, the above fact implies that the inferred models can be a satisfactory approximation to the actual structure. Figure 9 compares the transfer ratio for model OXF71-SE-B with those of models SE-B10U and SE-B10L in which the upper and lower boundaries of the 7.0-km/sec layer of model OXF71-SE-B are replaced by a transitional layer 10 km thick, respectively. In the actual computation, each 5-km interval above and below the boundary is divided into sublayers with 0.2-km thickness. This may give a good

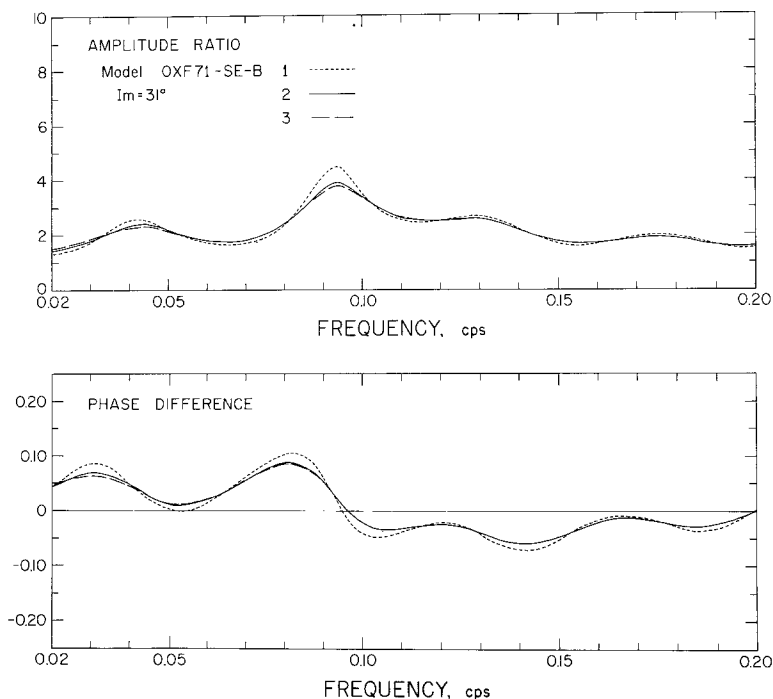


FIG. 10. Comparison of the nontruncated and truncated transfer ratios of model OXF71-SE-B: (1) $L_w(\omega)/L_u(\omega)$; (2) $L_w(\omega) \cdot W_1(\omega)/L_u(\omega) \cdot W_1(\omega)$; (3) $B(\omega)L_w(\omega)I(\omega) \cdot W_1(\omega)/B(\omega)L_u(\omega)I(\omega) \cdot W_1(\omega)$.

approximation to a smooth transitional layering. It appears from the figure that the lower boundary (Moho) consisting of a transitional layer of over 10-km thickness greatly suppresses the peaks at the higher frequencies, whereas a gradient for the upper boundary causes no decreases and sometimes even heightens peaks at the higher frequencies. Although not shown, a transitional layering of over 15-km thickness at the upper boundary and of over 20 km between the 6.3-km/sec layer and the Moho smooth out the fourth peak, while the transitional layer of over 5-km thickness at each or both boundaries does not bring about a substantial change in the height of peaks. From comparisons of observational ratios in Figure 4(c) with the transfer ratios above, and similar comparisons for the other best models, we may conclude that transitional layering thicker than about 5 km is unlikely for the Moho, but a gradient up to about 10-km thickness is

possible for the discontinuities in the lower crust. The above discussion is based on the replacement of a sharp discontinuity by a transitional layer in the inferred models. Therefore, a possibility remains that a quite different model with transitional layers will attain a better fit, but its possibility may be very low.

S-wave velocities have been assumed through an assumed Poisson's ratio of 0.26 for the crust and uppermost mantle. A decrease in Poisson's ratio generally lowers peaks and shifts them to higher frequencies, and an increase in Poisson's ratio causes a reverse effect. Poisson's ratio of about 0.25 to 0.26 may be appropriate to the crust and uppermost mantle for the region studied. A decrease in Poisson's ratio to 0.25 has little effect on the transfer ratio, and causes at most 1-km thinner crust. Possible variations in densities from values inferred from the relation (2) have a negligible effect.

Figure 10 compares the transfer ratio, $L_w(\omega)/L_u(\omega)$ which has been used above, with truncated transfer ratio, $L_w(\omega) \cdot W_1(\omega)/L_u(\omega) \cdot W_1(\omega)$ and $B(\omega)L_w(\omega)I(\omega) \cdot W_1(\omega)/B(\omega)L_u(\omega)I(\omega) \cdot W_1(\omega)$ which was formulated in Kurita (1973a), for model OXF71-SE-B. $L_w(\omega)$ and $L_u(\omega)$ show the vertical and horizontal motions of the transfer function, respectively. $W_1(\omega)$ is the spectral window corresponding to the data window, $w_1(t)$ having a time length of 80 sec which was used dominantly in the above analysis. $B(\omega)$ and $I(\omega)$ are the spectrum of the wave incident at the Moho (Kurita, 1973c), and the instrumental response, respectively. In computing $I(\omega)$, the critical damping is assumed from an examination of the calibration pulses. From this comparison and others not shown, it appears that the combined effect of the spectrum of the incident wave and the instrumental response is small, whereas the effect of truncation is rather marked. However, in the light of the present reliability of the observational ratio, it seems unnecessary to disqualify the models obtained above by the nontruncated transfer ratio method. More detailed studies of the crustal structure, based on the truncated transfer ratio, require more reliable observational ratio. They can possibly be obtained from analysis of high-quality records of deep earthquakes. It may be noteworthy to observe from a comparison of Figures 9 and 10 that the existence of the transitional layering in the crust dominantly changes the height of peaks at frequencies higher than about 0.10 Hz, while the effect of truncation mainly affects the height of peaks at frequencies lower than about 0.10 Hz.

CONCLUSIONS

The crustal structure in the central United States has been studied by the transfer ratio method from an analysis of teleseismic, long-period *P* waves recorded at SHA, OXF, FLO, and MDS. Since the inferred models are composed of homogeneous, isotropic, horizontal parallel layers and contain some assumed layer parameters, the actual structures around the stations are certainly different from the inferred models. As for the long-period waves with periods longer than about 5 sec, however, the dynamic response of these models can be almost equivalent to that of the actual structures.

The general features of the crustal structure in this region are summarized as follows:

(a) The crust is primarily approximated by a stack of horizontal parallel layers within about 100-km areas around SHA, OXF, and MDS. The crustal structure around FLO is rather complicated.

(b) The crust is about 33 km thick near the coast of the Gulf of Mexico (SHA), and thickens to about 41 km near an intersection of the Gulf coastal plain and the interior plain (OXF). It further thickens to about 47 km or more in the midst of the interior plain (FLO), and thins to about 41 km toward an intersection of the interior plain and the superior upland (MDS). As for the crust around FLO, however, its thickness reduces to about 42 km, if the *P*-wave velocity in the lower crust is taken as 7.0 km/sec instead of 7.4 km/sec.

(c) A sedimentary layer having a velocity of about 3.0 km/sec is confined to the Gulf coastal plain. This layer is about 3 km thick near the coast of the Gulf of Mexico, and tapers out to the north.

(d) A near-surface layer with a velocity of about 4.7 to 5.4 km/sec and having a thickness of about 1 to 3 km is a prevailing feature.

(e) In each of the regions referred to in (b), the thickness of the silicic upper crust with a velocity of about 6.0 to 6.5 km/sec is about 15, 30, 35, and 30 km, respectively.

(f) The mafic lower crust with a velocity of about 6.9 to 7.0 km/sec and having a thickness of about 10 km, is a common feature possibly except for the midst of the interior plain around FLO, where a velocity of about 7.4 km/sec is probable, implying an inclusion of ultramafic rocks.

(g) The uppermost mantle velocity of about 8.10 km/sec near the coast of the Gulf of Mexico increases to about 8.15 km/sec to the north.

(h) Deeper interfaces in the crust may possibly be replaced by the transitional layering up to 10 km thick.

(i) The crustal thickness is predominantly controlled by the silicic upper crust.

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